

# PROTOCOL PROGRAMMING WITH AUTOMATA: (WHY AND) HOW?

Sung-Shik Jongmans<sup>1,2,(3,4)</sup> (Farhad Arbab<sup>3,4</sup>)

<sup>1</sup>Open University, the Netherlands

<sup>2</sup>Radboud University, the Netherlands

<sup>3</sup>Centrum Wiskunde & Informatica, the Netherlands

<sup>4</sup>Leiden University, the Netherlands

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**Previous talk:** “We need a higher level of abstraction (than conventional stuff) for programming protocols.”

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**This talk:** “Here is one option.”

Running example: **Producers** / **consumer** protocol

Alice, Bob Carol

**Properties:** Asynchronous, reliable, unordered, transactional

```
public class Buffer {  
    public volatile Object content;  
    public final Semaphore empty = new Semaphore(1);  
    public final Semaphore full = new Semaphore(0);  
}
```

Typical implementation (Ben-Ari's textbook)

```
public class Producer extends Thread {
    private final Buffer buffer;

    public Producer(Buffer buffer) {
        this.buffer = buffer;
    }

    @Override
    public void run() {
        while (true) {
            Object datum = Thread.currentThread().getId();
            buffer.empty.acquire();
            buffer.content = datum;
            buffer.full.release();
        } } }
```

Typical implementation (Ben-Ari's textbook)

```
public class Consumer extends Thread {
    private final Buffer buffer;

    public Consumer(Buffer buffer) {
        this.buffer = buffer;
    }

    @Override
    public void run() {
        while (true) {
            buffer.full.acquire();
            Object datum = buffer.content;
            buffer.empty.release();
            System.out.println(datum);
        } } }
```

Typical implementation (Ben-Ari's textbook)

```
public class Program {  
    public static void main(String[] args) {  
        Buffer buffer = new Buffer();  
  
        Producer alice = new Producer(buffer);  
        Producer bob = new Producer(buffer);  
        Consumer carol = new Consumer(buffer);  
  
        alice.start();  
        bob.start();  
        carol.start();  
    } }  
}
```

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public interface InputPort {  
    public void put(Object datum);  
}
```

```
public interface OutputPort {  
    public Object get();  
}
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public interface InputPort {  
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- Processes are **oblivious** to data-flow.  
⇒ *That's what we have protocols for.*

```
public class Process {  
    public static void Producer(InputPort port) {  
        while (true) {  
            Object datum = Thread.currentThread().getId();  
            port.put(datum);  
        }  
    }  
  
    public static void Consumer(OutputPort port) {  
        while (true) {  
            Object datum = port.get();  
            System.out.println(datum);  
        }  
    }  
}
```

## Port-based implementation

```

public class Program {
  public static void main(String[] args) { // generated
    final InputPort A = Port.newInputPort();
    final InputPort B = Port.newInputPort();
    final OutputPort C = Port.newOutputPort();

    Thread alice = new Thread() {
      public void run() { Process.Producer(A) } }
    Thread bob = new Thread() {
      public void run() { Process.Producer(B) } }
    Thread carol = new Thread() {
      public void run() { Process.Consumer(C) } }

    alice.start();
    bob.start();
    carol.start();
  } }

```

## Port-based implementation



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public class Program {
    public static void main(String[] args) { // generated
        final InputPort A = Port.newInputPort();
        final InputPort B = Port.newInputPort();
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        (new Protocol(A,B,C)).start();

        Thread alice = new Thread() {
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        Thread bob = new Thread() {
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        alice.start();
        bob.start();
        carol.start();
    } }

```

## Port-based implementation

**Q:** Where does Protocol (A,B,C) come from?

**A:** Protocol (A,B,C) is specified in a DSL for protocols.

What are suitable  
programming constructs  
to denote such models?

**Approach:** First semantics, then syntax.

What are suitable  
models of interaction?

During a program run, put/get operations complete.

We call an *infinite* sequence of completions an **interaction**.

We call a set of *admissible* interactions a **protocol**.

An interaction is a function  $w : \mathbb{N} \rightarrow \underbrace{\mathbb{P} \rightarrow \mathbb{D}}_{\text{multiactions}}$

### Examples:

- $\{A \mapsto 0\}, \{C \mapsto 0\}, \{A \mapsto 1\}, \{C \mapsto 1\}, \{A \mapsto 2\}, \{C \mapsto 2\}, \dots$

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- $\{A \mapsto 0\}, \{B \mapsto 1\}, \{C \mapsto 0\}, \{C \mapsto 1\}, \dots$  [nontransactional]

A protocol is a set  $L \subseteq \mathbb{N} \rightarrow (\mathbb{P} \rightarrow \mathbb{D})$

**Example:**

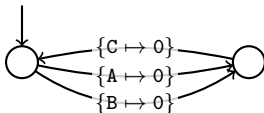
$$\left\{ w \left| \begin{array}{l} w : \mathbb{N} \rightarrow (\mathbb{P} \rightarrow \mathbb{D}) \\ \text{and } \left[ \begin{array}{l} \text{Dom}(w(i)) = \{A\} \\ \text{or } \text{Dom}(w(i)) = \{B\} \end{array} \right] \text{ for all } i \in \mathbb{N}_{\text{even}} \\ \text{and } [\text{Dom}(w(i)) = \{C\} \text{ for all } i \in \mathbb{N}_{\text{odd}}] \\ \text{and } [\text{Img}(w(i)) = \text{Img}(w(i+1)) \text{ for all } i \in \mathbb{N}_{\text{even}}] \end{array} \right. \right\}$$

Interactions are **words**; Protocols are **languages**.

**First attempt:** An automaton is a tuple  $(Q, P, \longrightarrow, q_0)$ ,  
where  $\longrightarrow \subseteq Q \times (P \rightarrow \mathbb{D}) \times Q$

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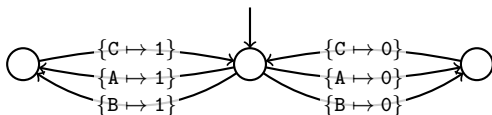
**Example:** Producers/consumer,  $\mathbb{D} = \{0\}$





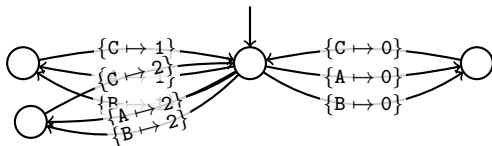
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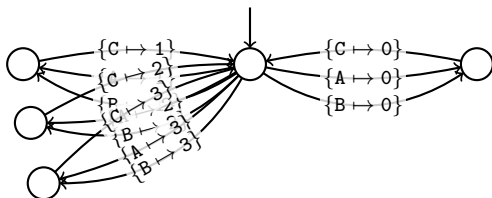
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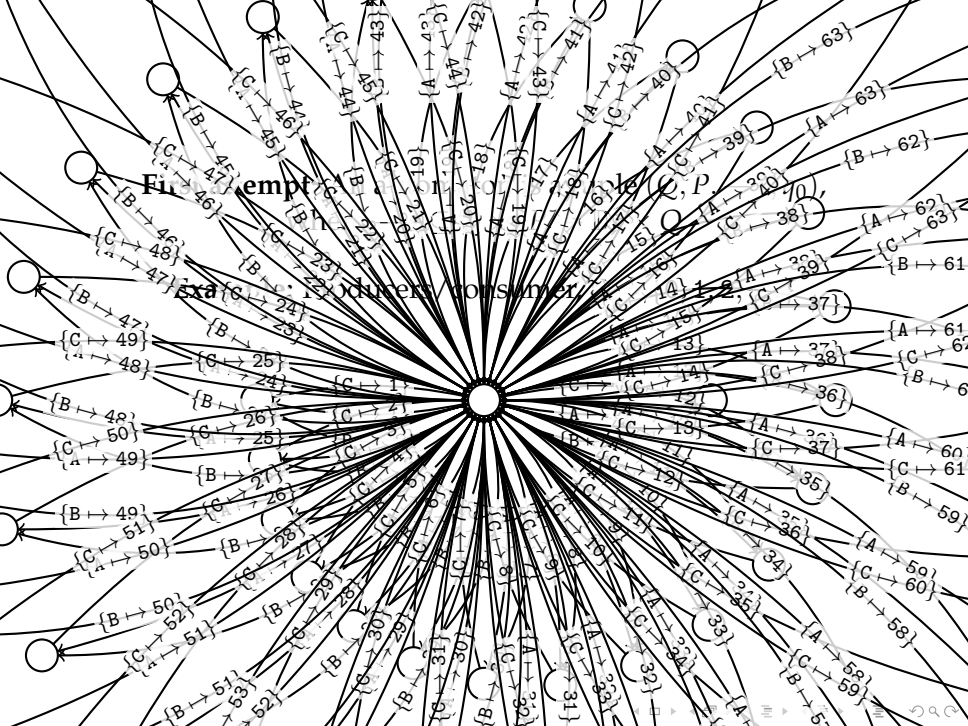
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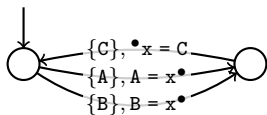




**Second attempt:** An automaton is a tuple  $(Q, P, M, \longrightarrow, q_0, \mu_0)$ ,  
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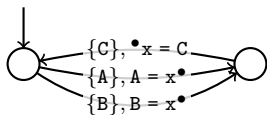
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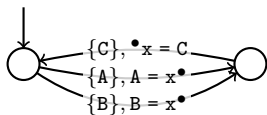
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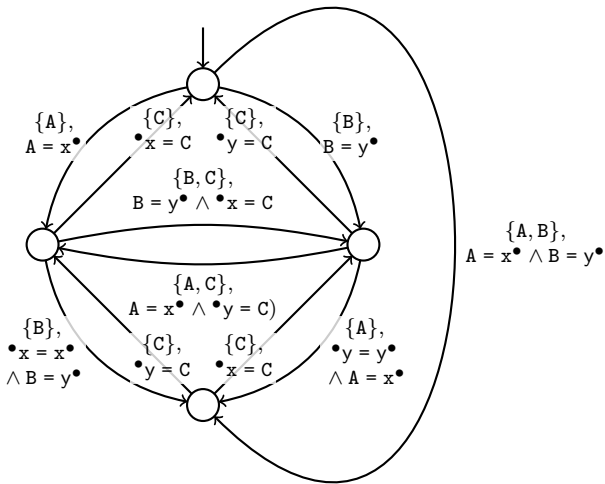
- **Instantaneous description:**  $(q, w, \mu)$ 
  - $q \in Q$  is the current state
  - $w : \mathbb{N} \rightarrow (P \rightarrow \mathbb{D})$  is the remaining word (“input tape”)
  - $\mu : M \rightarrow \mathbb{D}$  is the current content of memory cells (“stack”)

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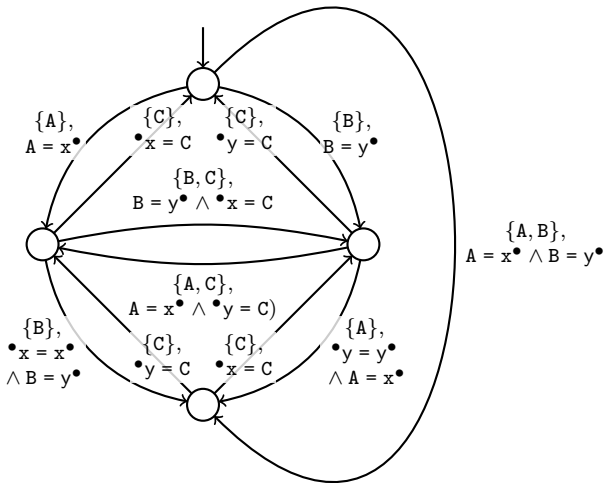
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- **Move:**  $(q, w, \mu') \vdash (q', w', \mu')$
- **Language:**  $\{w \mid (q_0, w, \mu_0) \vdash (q_1, w', \mu_1) \vdash (q_2, w'', \mu_2) \vdash \dots\}$   
 $\Rightarrow$  Automata model protocols, operationally.



Asynchronous, reliable, unordered, **nontransactional**

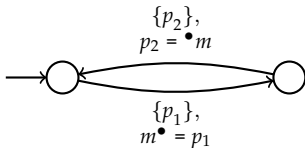
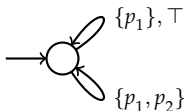


For  $k$  producers,  $2^k$  states and  $\mathcal{O}(k \cdot 2^k)$  transitions *per state*

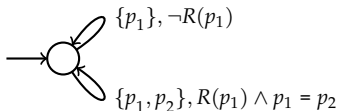
# Compositional construction, through **multiplication**

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$\{p_1, p_2\}, p_1 = p_2$



$\{p_1, p_2\}, f(p_1) = p_2$



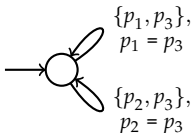
$\{p_1, p_2\}, R(p_1, p_2)$



$\{p_1, p_2, p_3\},$   
 $p_1 = p_2 \wedge p_1 = p_3$

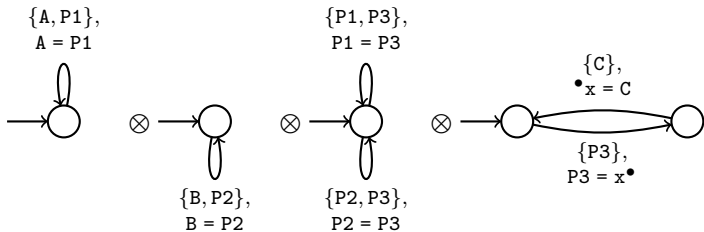


$\{p_1, p_2, p_3\},$   
 $f(p_1, p_2) = p_3$



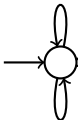


## Example:



## Example:

$\{A, P1\},$   
 $A = P1 \wedge K(\emptyset)$



$\{B, P2\},$   
 $B = P2 \wedge K(\emptyset)$

$\{A, B, P1, P2\},$   
 $A = P1 \wedge B = P2$

$\otimes$

$\{P1, P3\},$   
 $P1 = P3$



$\{P2, P3\},$   
 $P2 = P3$

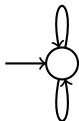
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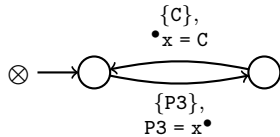
$\{C\},$   
 $\bullet x = C$   
 $\{P3\},$   
 $P3 = x \bullet$

## Example:

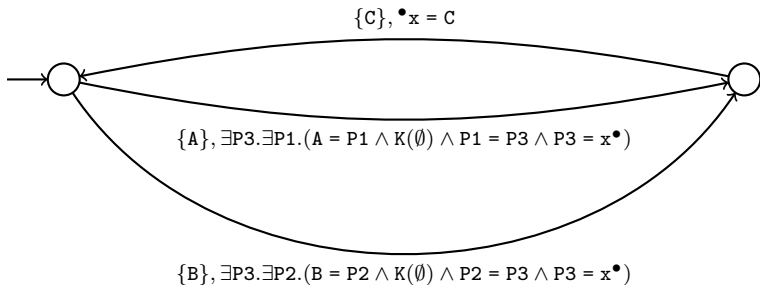
$$\{A, P3\},$$
$$\exists P1.(A = P1 \wedge K(\emptyset) \wedge P1 = P3)$$



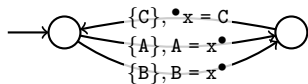
$$\{B, P3\},$$
$$\exists P2.(B = P2 \wedge K(\emptyset) \wedge P2 = P3)$$



## Example:



Example:



**Definition:**

$$\begin{pmatrix} Q_1, \\ P_1, \\ M_1, \\ \longrightarrow_1, \\ q_1^0, \\ \mu_1^0 \end{pmatrix} \otimes \begin{pmatrix} Q_2, \\ P_2, \\ M_2, \\ \longrightarrow_2, \\ q_2^0, \\ \mu_2^0 \end{pmatrix} = \begin{pmatrix} Q_1 \times Q_2, \\ P_1 \triangle P_2, \\ M_1 \cup M_2, \\ \longrightarrow, \\ (q_1^0, q_2^0), \\ \mu_1^0 \cup \mu_2^0 \end{pmatrix} \quad \text{if } M_1 \cap M_2 = \emptyset$$

where  $\longrightarrow$  is the smallest relation induced by the rules on the next slide.

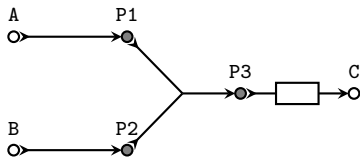
$$\frac{q_1 \xrightarrow{P_1^{\text{tr}}, \phi_1} q'_1 \text{ and } q_2 \xrightarrow{P_2^{\text{tr}}, \phi_2} q'_2 \text{ and } P_1 \cap P_2^{\text{tr}} = P_2 \cap P_1^{\text{tr}}}{q \xrightarrow{P_1^{\text{tr}} \Delta P_2^{\text{tr}}, \exists P_1^{\text{tr}} \cap P_2^{\text{tr}}. \phi_1 \wedge \phi_2} q'}$$

$$\frac{q_1 \xrightarrow{P_1^{\text{tr}}, \phi_1} q'_1 \text{ and } q_2 \in Q_2 \text{ and } P_2 \cap P_1^{\text{tr}} = \emptyset}{(q_1, q_2) \xrightarrow{P_1^{\text{tr}}, \phi_1 \wedge K(M_2)} (q'_1, q_2)}$$

$$\frac{q_2 \xrightarrow{P_2^{\text{tr}}, \phi_2} q'_2 \text{ and } q_1 \in Q_1 \text{ and } P_1 \cap P_2^{\text{tr}} = \emptyset}{(q_1, q_2) \xrightarrow{P_2^{\text{tr}}, \phi_2 \wedge K(M_1)} (q_1, q'_2)}$$

Syntax for multiplication expressions:

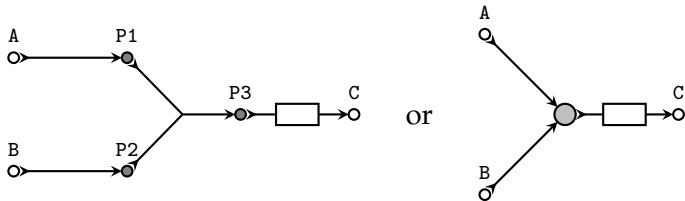
- **Graphical:** Every **edge** denotes an automaton.





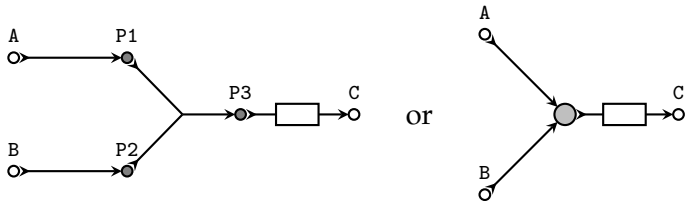
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Syntax for multiplication expressions:

- **Graphical:** Every **edge** denotes an automaton.



- **Textual:** Every **signature** denotes an automaton.

```
LateAsyncMerger(a,b;c) =  
  Sync(a;P1) mult Sync(b;P2) mult Merger2(P1,P2;P3) mult Fifo(P3;c)  
  
main = LateAsyncMerger(A,B;C)
```

Demo

## Compilation:

- 1 Extract a list of “**small**” automata from the syntax.
- 2 Multiply those automata into one “**big**” automaton.
- 3 Translate that automaton into state machine code.

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I need **four chapters** of optimizations to get *some* performance.

That's it.

Questions?