



Are Some Voters More Equal Than Others?

Discussions and work in progress on formalisation

Hugo Jonker

in collaboration with Ben Smyth



Elections:

a way to establish the preference of a group,
based on the preferences of the individual members.



Elections:

a way to establish the preference of a group,
based on the preferences of the individual members.

1. Collect individual preferences.



Elections:

a way to establish the preference of a group,
based on the preferences of the individual members.

1. Collect individual preferences.
2. Derive group preference.



Elections:

a way to establish the preference of a group,
based on the preferences of the individual members.

- 1. Collect individual preferences.**
2. Derive group preference.



Are all voters equal?

- Who votes first?
- Who votes last?

Shouldn't matter, but:



Are all voters equal?

- Who votes first?
- Who votes last?

Shouldn't matter, but:

- Last voter knows 2 major parties are precisely tied.
⇒ last voter can determine winner.
- Eurovision song festival voting: why vote for a losing party?



Are all voters equal?

- Who votes first?
- Who votes last?

Shouldn't matter, but:

- Last voter knows 2 major parties are precisely tied.
⇒ last voter can determine winner.
- Eurovision song festival voting: why vote for a losing party?

Elections should be **fair**.



Fairness = each participant has equal “opportunity”.

In other fields:



Fairness = each participant has equal “opportunity”.

In other fields:

- **computation:**

- every path must occur in an infinite computation.

- **contract signing:**

- Either all or none of the parties receive a signed document.

- **two-party exchange:**

- Either both items change owner, or neither does.



Fairness in voting

- A voting system doesn't confer any advantage upon any voter.



Fairness in voting

- A voting system doesn't confer any advantage upon any voter.
- A voting system doesn't allow any voter an advantage.



Fairness in voting

- A voting system doesn't confer any advantage upon any voter.
- A voting system doesn't allow any voter an advantage.
- No pulling out (cf. [FOO92]).



Fairness in voting

- A voting system doesn't confer any advantage upon any voter.
- A voting system doesn't allow any voter an advantage.
- No pulling out (cf. [FOO92]).
- All voters have “similar” information about how their vote affects the result.



Fairness in voting

- A voting system doesn't confer any advantage upon any voter.
- A voting system doesn't allow any voter an advantage.
- No pulling out (cf. [FOO92]).
- All voters have “similar” information about how their vote affects the result.
- All voters know in advance how to obtain the advantage.



- A voting system doesn't confer any advantage upon any voter.
- A voting system doesn't allow any voter an advantage.
- No pulling out (cf. [FOO92]).
- All voters have “similar” information about how their vote affects the result.
- All voters know in advance how to obtain the advantage.

Each voter has specific, partial control over the result.

Fairness is broken when a voter can exercise control beyond this.

Control: “+1”? can vary per voter?



Examples for discussion



Situation 1 (*copy ballot*):

Submit a copy of another voter's filled in ballot.

- You can vote the same as someone.
- Privacy problem? fairness problem?



Situation 1 (*copy ballot*):

Submit a copy of another voter's filled in ballot.

- You can vote the same as someone.
- Privacy problem? fairness problem?

Situation 2 (*vote unlike someone*):

*Submit a **modified** copy of another voter's filled in ballot.*

- You can vote unlike someone.
- Privacy problem? Fairness problem?



Discussion: aborting a vote

Situation 3 (*change your mind*):

If voting occurs in > 1 phase, don't participate in last phase.

- You can cancel your vote.
- When is this a fairness problem?



Existing formalisations



[KR05]: to verify [FOO92].

- no one can learn vote v before opening phase.
Standard ProVerif secrecy check of vote variable v .
- no one can guess v before opening phase. $\phi \approx_s \nu v.\phi$ – ProVerif check.

+ automatic checking

- copying/modifying ballot not caught
- contents of vote $\xRightarrow{?}$ no early results



BRS07: no early results

[BRS07]: to verify [FOO92].

$$\neg \text{resultAnnounced} \implies \bigwedge_{a \in Ag} L_a \left(\bigwedge_{b \neq a, c \in \mathcal{C}} \text{vote}_b(c) \right).$$

Before results, no one can exclude any choice by any other voter.

- + knowledge based reasoning
- + straightforward definition
- how to apply
- fairness > knowing no ballots



[TMT⁺08]: case study of [FOO92].

$$\nu X. \bigwedge_{c \in \mathcal{C}} (\langle x.(x_i - X_s \triangleright X_r : v).y \varphi \rightarrow \varepsilon \rangle tt \rightarrow \\ \langle x.d(T).y.(x_i - X_s \triangleright X_r : v).z \varphi \rightarrow x.d(T).y.z \rangle X))$$

If a vote can be determined, then there must have been a phase boundary earlier in the protocol.

- “normalized” protocol
- non-intuitive language
- guessing attacks not caught
- ballot exposure \neq fairness



BHM08: don't re-use the vote

[BHM08]: general def of “soundness”, applied to [JCJ05].

Every eligible voter votes once.

- $t = t1 \cdot \text{start}(id) \cdot t2$.
- Eligibility: $\text{start}(id) \notin t1 \cdot t2$.
- One vote: $\text{newid}(id) \in t1$. (event by id manager).

+ simple, straightforward def

- limited to “soundness” / accuracy + democracy



Towards formalising fairness



If the result is unaffected, fairness is not harmed.



1. before voting, voter observes trace t ;
2. t can be extrapolated to full run with and without voter;
3. For all such possible extrapolations: determine result;

Fairness: $\exists c: \forall t \in Tr(with): \exists t' \in Tr(without): c = \text{result}(t) - \text{result}(t') \wedge t \approx t'$.



- Constant = 1,2,3,...
- Difference between two results constant necessary? Sufficient?
- What if no one votes after voter? Or a variable number?



Possible definitions of fairness:

a.i. Result occurs > 1 **before** casting, not possible **after**:
 \implies fairness violated.



Possible definitions of fairness:

a.i. Result occurs > 1 **before** casting, not possible **after**:
 \implies fairness violated.

a.ii. Distribution of result changed by > 1 (vote) after casting:
 \implies fairness violated.



Possible definitions of fairness:

a.i. Result occurs > 1 **before** casting, not possible **after**:
 \implies fairness violated.

a.ii. Distribution of result changed by > 1 (vote) after casting:
 \implies fairness violated.

b.i. For every voter, the effect should be the same.



Possible definitions of fairness:

a.i. Result occurs > 1 **before** casting, not possible **after**:
 \implies fairness violated.

a.ii. Distribution of result changed by > 1 (vote) after casting:
 \implies fairness violated.

b.i. For every voter, the effect should be the same.

b.ii. For every voter, the effect should be the same:
A change of 1 vote.



Possible definitions of fairness:

a.i. Result occurs > 1 **before** casting, not possible **after**:
 \implies fairness violated.

a.ii. Distribution of result changed by > 1 (vote) after casting:
 \implies fairness violated.

b.i. For every voter, the effect should be the same.

b.ii. For every voter, the effect should be the same:
A change of 1 vote.

c. The voting system does not influence the vote.



Possible definitions of fairness:

a.i. Result occurs > 1 **before** casting, not possible **after**:
 \implies fairness violated.

a.ii. Distribution of result changed by > 1 (vote) after casting:
 \implies fairness violated.

b.i. For every voter, the effect should be the same.

b.ii. For every voter, the effect should be the same:
A change of 1 vote.

c. The voting system does not influence the vote.

d. No pulling out (problem in FOO).



Conclusions

- Fairness is necessary for fair voting systems, ...
- ...and we can formally express something,...
- ... but do we know what fairness is?



Conclusions

- Fairness is necessary for fair voting systems, ...
- ...and we can formally express something,...
- ... but do we know what fairness is?

Thank you for your attention.

Questions/comments?



References

- [BHM08] M. Backes, C. Hrițcu, and M. Maffei. Automated verification of remote electronic voting protocols in the applied pi-calculus. In Proc. 21st IEEE Computer Security Foundations Symposium, pages 195–209. IEEE Computer Society, 2008.
- [BRS07] A. Baskar, R. Ramanujam, and S. P. Suresh. Knowledge-based modelling of voting protocols. In Proc. 11th Conference on Theoretical Aspects of Rationality and Knowledge, pages 62–71. ACM, 2007.
- [FOO92] A. Fujioka, T. Okamoto, and K. Ohta. A practical secret voting scheme for large scale elections. In Advances in Cryptology – AUSCRYPT '92, volume 718 of LNCS, pages 244–251. Springer, 1992.
- [JCJ05] A. Juels, D. Catalano, and M. Jakobsson. Coercion-resistant electronic elections. In Proc. 2005 ACM Workshop on Privacy in the Electronic Society, pages 61–70. ACM, 2005.
- [KR05] S. Kremer and M. Ryan. Analysis of an electronic voting protocol in the applied pi calculus. In Proc. 14th European Symposium on Programming, volume 3444 of LNCS, pages 186–200. Springer, 2005.